- X_2 mole fraction of the second component, i.e., solvent
- mole fraction of the acid in vapor phase V

Registry No. (CH3)2CHCOOH, 79-31-2; (CH3)3CCOOH, 75-98-9; c-C6H12, 110-82-7; n-C7H18, 142-82-5.

Literature Cited

- (1) Lark, B. S.; Banipai, T. S.; Singh, S.; Palta, R. C. J. Chem. Eng. Data 1984, *29*, 277-80
- (2)Lark, B. S.; Banipal, T. S.; Singh, S. J. Chem. Eng. Data 1985, 30, 286-88
- (3) Miksch, G.; Ratkovics, F.; Kohler, F.; J. Chem. Thermodyn. 1969, 1, 257-65.
- (4) Kohler, F.; Atrops, H.; Kaloll, E.; Libermann, E.; Wilhelm, E.; Ratkovics, F.; Salemon, T. *J. Phys. Chem.* **1981**, *85*, 2520–24. Taylor, M. D. *J. Am. Chem. Soc.* **1951**, *73*, 315–17. Lark, B. S.; Banipal, T. S. *Thermochim. Acta* **1985**, *91*, 141–49.
- (6) Singh, Tarlok., Ph.D. Thesis, Guru Nanak Dev University, Amritsar, In-(7)
- dia, 1986.
- (8) Lark, B. S.; Palta, R. C. Malaysian J. Sci. 1980, 6(B), 159-65.

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Predicting Refractive Index and Density Increments of Binary Solvent Mixtures

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Refractive indices and densities of six binary liquid mixtures measured at 20 °C for three wavelengths (589, 546, and 436 nm) have been used to predict their increments. Dependence of refractive index and density increments has been discussed as a function of composition of the mixture.

For a satisfactory thermodynamic treatment of polymers in mixed solvents it seemed important to have accurate values of refractive index and density increments (1-3). While these increments can be measured experimentally for polymer solutions, no accurate procedure exists to measure them in neat solvent mixtures. In this study, an attempt is made to present equations which could be successfully used to predict both refractive index and density increments of solvent mixtures by using refractive index and density data on pure solvents and their mixtures. Accordingly, refractive indices and densities have been measured for six binary mixtures comprising benzene, cyclohexane, ethyl acetate, and carbon tetrachloride at 20 °C over the entire range of composition for each mixture. The data are used to predict refractive index and density increments of solvent mixtures; a dependence of these quantities on mixture composition is also discussed.

Theory

To incorporate the changes of volume and refractivity, we use the following relations (2, 4)

$$\Delta V_{\rm mix} = (\sum_{i=1}^{2} N_i V_i) A_{12} \phi_1 \phi_2$$
(1)

$$\Delta \boldsymbol{R}_{mix} = \left(\sum_{i=1}^{2} N_i V_i\right) \boldsymbol{B}_{12} \phi_1 \phi_2 \tag{2}$$

where A_{12} and B_{12} are the empirical parameters which depend on composition of the mixture; ϕ_i is the volume fraction of the ith component in a mixture.

Lorentz-Lorenz relation leads to the definition of molar refractivity, R_i , of pure substance *i* as (5)

$$R_{i} = [(n_{i}^{2} - 1)/(n_{i}^{2} + 2)](M_{i}/\rho_{i})$$
(3)

where n_i , M_i , and ρ_i represent the refractive index, molecular

weight, and density of the *i*th component in the mixture. However, the refractivity, R, of a mixture is defined as the product of polarizability P and volume V of the system (6). Thus

$$R \equiv PV \tag{4}$$

so that

$$P \equiv (n^2 - 1) / (n^2 + 2) \tag{5}$$

where *n* is the refractive index of the mixture. For binary mixtures the following relations are feasible

$$\rho = (\phi_1 \rho_1 + \phi_2 \rho_2) / (1 + A_{12} \phi_1 \phi_2)$$
(6)

$$P = (\phi_1 P_1 + \phi_2 P_2 + B_{12} \phi_1 \phi_2) / (1 + A_{12} \phi_1 \phi_2)$$
(7)

where P1, P2 are the polarizability of component 1 and 2 of the mixture; ρ_1 , ρ_2 and ϕ_1 , ϕ_2 represent their respective densities and volume fractions. Routine calculations from eq 6 and 7 lead to the desired quantities

$$(d\rho/d\phi_1) = \frac{(\rho_1 - \rho_2) + \rho D}{(1 + A_{12}\phi_1\phi_2)}$$
(8)

$$(dn/d\phi_1) = \left[(n^2 + 2) \left\{ \left[(P_1 - P_2) + B_{12}(\phi_2 - \phi_1) + \frac{dB_{12}}{d\phi_1} (\phi_1 \phi_2) \right] - PD \right\} \right] / [6n(1 + A_{12}\phi_1\phi_2)]$$
(9)

where

$$D = \left[A_{12}(\phi_2 - \phi_1) + \frac{dA_{12}}{d\phi_1} (\phi_1 \phi_2) \right]$$

Experimentally calculated values of A_{12} and B_{12} (using eq 6 and 7) may be fitted to the following quadratic equations in order to evaluate the coefficients a_0 , a_1 , a_2 , and b_0 , b_1 , and b_2 .

$$A_{12} = a_0 + a_1(\phi_2 - \phi_1) + a_2(\phi_2 - \phi_1)^2$$
(10)

$$B_{12} = b_0 + b_1(\phi_2 - \phi_1) + b_2(\phi_2 - \phi_1)^2$$
(11)

Equations 10 and 11 are used to compute the derivatives $(dA_{12}/d\phi_1)$ and $(dB_{12}/d\phi_1)$ whose values are then inserted into eq 8 and 9 along with others to predict the incremental values



Figure 1. Dependence of density on volume fraction of the first-named component in the mixture at 20 °C: (Δ) cyclohexane (1)-carbon tetrachloride (2); (∇) benzene (1)-carbon tetrachloride (2); (∇) ethyl acetate (1)-carbon tetrachloride (2); (\Box) benzene (1)-ethyl acetate (2); (O) benzene (1)-cyclohexane (2); (\bullet) ethyl acetate (1)-cyclohexane (2); (\bullet) ethyl ethy

of density and refractive index.

Experimental Section

Solvents used in this work were of reagent grade and were used without further purification. Gas chromatography did not show any impurity except for cyclohexane. Different batches of cyclohexane contained about 0.2-1% impurity and their physical properties varied accordingly. However, each series of experiments was performed with a single batch of cyclohexane and the values of density and refractive index applicable to each batch were used for its evaluation. Solvent mixtures were prepared by weighing appropriate volumes of pure solvents. The volume fractions were calculated from the weights and densities of pure components (1).

Densities were measured at 20 \pm 0.01 °C with a precision density meter, Model DMA 02C, manufactured by Anton Paar K.G., Austria. A Bausch and Lomb precision refractometer was used to measure the refractive index. The instrument was equipped with mercury and sodium light sources. The precision of the instrument is \pm 0.000 03 units. Samples were applied to the prism of the refractometer as quickly as possible to minimize evaporation and accompanying changes in composition of the mixture. Measurements were done at 20 \pm 0.01 °C by using sodium (589 nm) line, mercury green (546 nm), and blue (436 nm) lines. The experimental data reported here were collected at the university of Texas, Austin, TX (courtesy of Professor Petr Munk).

Results and Discussion

Densities, refractive indices, and their increments as calculated from eq 8 and 9, respectively, are compiled in Table I.



Figure 2. Dependence of refractive index on volume fraction of the first-named component in the mixture at 20 °C (symbols have the same meaning as in Figure 1): dotted line (436 nm); dashed line (546 nm); full line (589 nm).



Figure 3. Dependence of refractive index increment on volume fraction of the first-named component in the mixture at 20 °C: (∇) benzene (1)-ethyl acetate (2); (\square) benzene (1)-cyclohexane (2); (O) benzene (1)-carbon tetrachloride (2); (\triangle) cyclohexane (1)-carbon tetrachloride (2); (Θ) ethyl acetate (1)-cyclohexane (2); (∇) ethyl acetate (1)-carbon tetrachloride (2) (lines have the same meaning as in Figure 2).

Dependence of density on volume fraction (ϕ_1) of the mixture is shown in Figure 1. Mixtures of carbon tetrachloride with benzene, cyclohexane, or ethyl acetate and also benzene (1)-ethyl acetate (2) exhibit linear dependence. However, a slight deviation from straight-line behavior is shown by mixtures

Table I.	Densities, F	Refractive	Indices, a	and Density	and Refractive	Index I	ncrements fo	or Binary	Mixtures at 2	0 °C
1 4010 11	Transing at 1					I HUVA I	HOT OTHORDS IN			~ ~

	,	~~~~~										
	density,		retract. index		density	refra	ct. index incre	ment				
ψ,	g/cm^{3}	589 nm	546 nm	436 nm	increment	589 nm	546 nm	436 nm				
7 1	0/		TD	(1) 11.1	A (0)							
i, Benzene (1)-Etnyi Acetate (2)												
1.0	0.87916	1.50111	1.50521	1.52303								
0.9	0.88073	1.48756	1.49134	1.50792	-0.0162	0.1349	0.1375	0.1497				
0.8	0.882 09	1.47393	1.47740	1.49278	-0.0183	0.1327	0.1352	0.1471				
0.7	0 884 41	1 460 84	1 464 13	1.478.35	~0.0200	0.1307	0.1331	0 1448				
0.1	0.886.38	1 147 80	1 450 73	1 463 79	-0.0213	0.1288	0 1313	0.1427				
0.0	0.000 50	1.447.00	1.40070	1,40070	0.0210	0.1200	0,1013	0.1427				
0.5	0.888.59	1.434 85	1.43770	1.44961	-0.0223	0.1272	0.1297	0.1409				
0.4	0.89085	1.42206	1.42457	1.43538	-0.0232	0.1258	0.1282	0.1393				
0.3	0.89311	1.40955	1.41180	1.42153	-0.0239	0.1246	0.1270	0.1379				
0.2	0.89559	1.39696	1.39902	1.40759	-0.0246	0.1236	0.1261	0.1368				
0.1	0.898.08	1 384 65	1 386 38	1,393,95	-0.0255	0.1228	0.1253	0.1359				
0.1	0.000.69	1.004.00	1.000.00	1 280 27	0.0200	0.1220	0.1200	0.1000				
0.0	0.900.66	1.07220	1.07002	1.000.27								
II. Benzene (1)-Carbon Tetrachloride (2)												
1.0 0.87916 1.50111 1.50521 1.52203												
1.0	0.87916	1.50111	1.50521	1.523.03								
0.9	0.95114	1.49719	1.50110	1.51817	-0.7186	0.0371	0.0387	0.0462				
0.8	1.02231	1.49340	1.49719	1.51350	-0.7166	0.0366	0.0382	0.0458				
0.7	1.094.26	1.48946	1,49310	1.50860	-0.7152	0.0364	0.0380	0.0466				
0.6	1 165 44	1.105 10	1 488 07	1.502.74	-0.7144	0.0365	0.0389	0.0461				
0.0	1.100 44	1.400.07	1.400 51	1.000 74	-0.7144	0.0000	0.0302	0.0401				
0.5	1.23699	1.48153	1.484.72	1.49871	-0.7143	0.0371	0.0388	0.0469				
0.4	1.30830	1.47742	1.48045	1.49363	-0.7146	0.0380	0.0398	0.0480				
0.3	1 379 33	1 473 20	1 476 05	1 488 39	-0.7151	0.0393	0.0411	0.0494				
0.0	1.070.00	1,400.01	1.471.00	1,400,00	0.7101	0.0000	0.0411	0.0404				
0.2	1.45110	1.468.91	1.4/163	1.483.08	-0.7156	0.0410	0.0428	0.0513				
0.1	1.52268	1.46456	1.46703	1.47763	-0.7155	0.0430	0.0449	0.0535				
0.0	1.59427	1.46003	1.46239	1.47214								
		=	-									
			III. Bei	nzene (1)-Cyclo	hexane (2)							
1.0	0.879.16	1 501 11	1 505 21	1 523 03								
0.0	0.07010	1.00111	1.000.21	1.510.00	0.1179	0.0071	0.0005	0.0002				
0.9	0.86730	1.49241	1.496.34	1.513.02	0.1173	0.0871	0.0895	0.0995				
0.8	0.85580	1.48382	1.48752	1.50312	0.1144	0.0853	0.0876	0.0955				
0.7	0.84459	1.47561	1.47901	1.49357	0.1108	0.0831	0.0853	0.0918				
0.6	0.833.81	1 467 67	1 470 82	1 484 33	0.1067	0.0805	0.0828	0.0884				
0.0	0.033.01	1.407.07	1.470.02	1.404.00	0.1007	0.0000	0.0020	0.0004				
0.ā	0.82344	1.45993	1.46287	1.47536	0.1023	0.0776	0.0799	0.0851				
0.4	0.81352	1.45252	1.45522	1.46671	0.0975	0.0745	0.0767	0.0820				
0.3	0.804.15	1 44554	1.44802	1.45847	0.0925	0.0710	0.0732	0.0790				
0.0	0.705.96	1 499 90	1 441 14	1 150 64	0.0874	0.0672	0.0694	0.0763				
0.2	0.790.20	1.430.00	1.44114	1,400.04	0.0074	0.0072	0.0054	0.0705				
0.1	0.786 70	1.43230	1.434 46	1.44306	0.0823	0.0632	0.0654	0.0737				
0.0	0.77876	1.42626	1.42811	1.43573								
			IV. Ethyl	Acetate (1)-Cy	clohexane (2)							
1.0	0.90068	1.37226	1.37382	1.38027								
0.9	0.885.42	1 375 85	1 377 51	1 384 04	0.1505	-0.0417	-0.0419	-0.0428				
0.0	0.000 42	1.070.00	1.001.50	1,0010	0.1000	0.0476	0.0470	0.0420				
0.8	0.870.64	1.379 99	1.381.96	1.30010	0.1448	-0.0476	-0.0479	-0.0488				
0.7	0.85653	1.38422	1.38589	1.39259	0.1394	-0.0526	-0.0528	0.0539				
0.6	0.84302	1.38892	1.39059	1.39735	0.1339	-0.0568	-0.0571	-0.0582				
0.5	0.830.23	1 393 95	1.395.67	1 402 57	0.1277	-0.0605	-0.0608	-0.0620				
0.0	0.00020	1,000.00	1.401.00	1.10207	0.1005	0.0000	0.0000	0.0657				
0.4	0.81817	1.399.37	1.401.06	1.40814	0.1205	-0.0641	-0.0644	-0.0657				
0.3	0.80687	1.40510	1.40681	1.41395	0.1117	-0.0678	-0.0682	-0.0695				
0.2	0.796.26	1.41137	1.41316	1.42045	0.1011	-0.0720	-0.0724	-0.0739				
0.1	0 786 71	1 418 39	1 420 15	1.497.61	0.0882	-0.0771	-0.0775	-0.0791				
0.1	0.70071	1.410.007	1 400 000	1.427.01	0.0002	0.0771	0.0110	0.0751				
0.0	0.77876	1.420 22"	1.428.09*	J.430/2°								
V. Ethyl Acatata (1) Carbon Tatrashlavida (0)												
1.0	0 000 60	1 979 96	1 070 00	1 220.07								
1.0	0.00000	1.000.05	1.010.04	1.000.27	0.0001	0.0005	0.0071	0.0000				
0.9	0.96984	1.380.85	1.38242	1.389.15	-0.6931	-0.0865	-0.0871	-0.0900				
0.8	1.03947	1.38954	1.39120	1.39824	-0.6930	-0.0873	-0.0878	-0.0908				
0.7	1.10834	1.39820	1.39987	1.40728	-0.6929	-0.0879	0.0885	-0.0916				
0.B	1 177 59	1 406 88	1 408 70	1 416 38	-0.6928	-0.0885	-0.0891	-0.0922				
0.0	1.040.00	1 415 00	1 417 50	1 495 05	0.0020	0.0000	0.0001	0.0022				
0.5	1.24088	1,410.06	1.41708	1.423 00	-0.6930	-0.0890	-0.0890	-0.0928				
0.4	1.31636	1.42447	1.42641	1.43476	-0.6934	-0.0893	-0.0901	-0.0934				
0.3	1.38465	1.43316	1.43516	1.44387	-0.6943	-0.0900	-0.0904	-0.0938				
0.9	1 454 87	1 442 04	1 444 18	1 453 21	-0.6958	-0.0897	-0.0906	-0.0941				
0.2	1 204 00	1 451 04	1 159 05	1 12020	-0.6090	_0.0001	_0.0000	-0.0011				
0.1	1.524.28	1.401.04	1.403 27	1.402.02	-0.0902	-0.0090	-0.0909	-0.0944				
0.0	1.59427	1.46003	1.46239	1.47214								
$\mathbf{M} = \{1, 2, \dots, 3\} = \{1, 2, \dots, 3\}$												
	المتعارين والمسترين		vi. Cyclohexa	ine (1)-Carbon	1 etrachioride (2)							
1.0	0.77866°	1.42624^{o}	1.42808^{o}	1.43573								
0.9	0.85949	1.42932	1.43115	1.43900	-0.8118	-0.0330	-0.0335	-0.0355				
0.8	0.941.39	1 439 57	1 434 47	1,449.54	-0.8134	-0.0349	-0.0354	-0.0375				
0.0	1 000 20	1 495 00	1 /97 07	1 446 14	_0 01 4 4	_0.0045	_0.0070	_0.0900				
0.7	1.023 62	1.400 90	1.43/8/	1,440 14	-0.0144	-0.0300	-0.0370	-0.0380				
0.6	1.10362	1.43924	1.441.20	1.44968	-0.8149	-0.0376	-0.0381	-0.0402				
0.5	1.18463	1.44254	1.44457	1.45327	-0.8151	-0.0383	-0.0388	-0.0409				
04	1.266.07	1.446.02	1.448.08	1.457.01	-0.8155	-0.0389	-0.0397	-0.0412				
n 9	1 947 94	1 440 46	1 451 61	1 460 70	-0.8168	-0.0384	-0.0300	-0.0411				
v.a 	1.04/04	1 450 00	1.455.01	1.40070	0.0100	0.0004	0.0000	0.0411				
0.2	1.42977	1.45299	1.45521	1.46451	-0.8201	-0.0379	-0.0384	-0.0406				
0.1	1.51118	1.45652	1.45876	1.46829	-0.8263	-0.0369	-0.0375	-0.0397				
(), Ô	1.59427	1.46003	1.46239	1.47214								

^a For the batch of cyclohexane used for the ethyl acetate (1)-cyclohexane (2) mixture. ^b For the batch of cyclohexane used for the cyclohexane (1)-carbon tetrachloride (2) mixture.



Figure 4. Dependence of density increment on volume fraction of the first-named component in the mixture at 20 °C: (O) benzene (1)cyclohexane (2); (●) ethyl acetate (1)-cyclohexane (2); (△) benzene (1)-carbon tetrachloride (2); (A) ethyl acetate (1)-carbon tetrachloride (2); (□) benzene (1)-ethyl acetate (2); (◊) cyclohexane (1)-carbon tetrachioride (2).

of cyclohexane with benzene or ethyl acetate.

Variation of refractive index for all the three wavelengths (589, 546, and 436 nm) as a function of ϕ_1 is shown in Figure 2. As expected, refractive index is higher for the mercury blue line (436 nm) than the mercury green line (546 nm). However, for sodium vellow line (589 nm) lower values of refractive indices than at either 546 or 436 nm are observed. For all the systems, the refractive index versus ϕ_1 curves are slightly deviated from a straight-line behavior.

Dependence of refractive index increment on ϕ_1 is shown in Figure 3. Mixtures of benzene with ethyl acetate, carbon tetrachloride or cyclohexane exhibit positive values for the increment for all the wavelengths. However, mixtures of ethyl acetate with cyclohexane or carbon tetrachloride and cyclohexane (1)-carbon tetrachloride (2) exhibit negative refractive index increments. In all the cases, the refractive index increments have shown increasing tendencies with a decrease in wavelength. The highest (and positive) values of refractive index increments are observed for the benzene (1)-ethyl acetate (2) system and the lowest (and negative) values are observed in the case of cyclohexane (1)-carbon tetrachloride (2) system. No strict linearity is observed for any of the systems as seen in Figure 3.

Dependence of density increment on volume fraction of the first component of the mixture is shown in Figure 4. For the systems benzene (1)-ethyl acetate (2), benzene (1)-carbon tetrachloride (2), ethyl acetate (1)-carbon tetrachloride (2), and cyclohexane (1)-carbon tetrachloride (2), the density increment is negative over the entire range of composition of the mixture. However, for the systems benzene (1)-cyclohexane (2) and ethyl acetate (1)-cyclohexane (2), the density increment is positive; for the latter system it is largest of all. For mixtures exhibiting positive refractive index increments the density increment is negative (see, for instance, mixtures I and II given in Table I). A reverse situation exists in the case of ethyl acetate (1)-cyclohexane (2) wherein the density increment is positive but refractive index increment is negative. On the other hand, for a few mixtures (see, for instance, mixtures V and VI given in Table I) both the increments are negative; in one case (mixture III) both the increments are positive. Thus, there appears to be no strict correlation between either the sign or magnitudes of these increments. From a general observation, it is apparent that if the first component of the mixture possesses higher values of either density or refractive index than the second component, then the increments are found to be positive. If on the other hand, the first component has lower values than the second then negative values of the increments are prevalent.

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Registry No. Benzene, 71-43-2; cyclohexane, 110-82-7; ethyl acetate, 141-78-6; carbon tetrachloride, 56-23-5.

Literature Cited

- (1) Aminabhavi, T. M.; Munk, P. Macromolecules 1979, 12, 607.
- Aminabhavi, T. M.; Munk, P. *Macromolecules* **1979**, *12*, 001. Aminabhavi, T. M.; Munk, P. *Macromolecules* **1979**, *17*, 879. (2)
- (3) Aminabhavi, T. M. J. Chem. Educ. 1983, 60, 117
- Huglin, M. B., Ed. Light Scattering from Polymer Solutions; Academic: (5)
- New York, 1972. (6) Letcher, T. M.; Bayles, J. W. J. Chem. Eng. Data 1971, 16, 266.

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Densities and Viscosities of Binary Liquid Mixtures at 45 $^\circ$ C

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Densities and viscosities for 14 binary liquid mixtures comprising carbon tetrachioride, cyclohexane, methyl ethyl ketone, benzene, p-xylene, bromobenzene, dimethyl sulfoxide, dimethylformamide, nitromethane, ethyl acetate, and methanol at 45 °C over the whole range of mixture compositions are presented.

Introduction

In our earlier studies (1-3) densities and viscosities have been measured at 25 and 35 °C for several binary mixtures

comprising carbon tetrachloride, cyclohexane, methyl ethyl ketone, dimethyl sulfoxide, dimethylformamide, nitromethane, benzene, bromobenzene, ethyl acetate, p-xylene, and methanol. In continuation of this research we now present additional data of densities and viscositites of 14 binary mixtures comprising the same solvents. The properties were studied over the entire range of composition of the mixture.

Experimental Section

All chemicals used were of commercial products of the highest available purity (BDH). These were further purified by